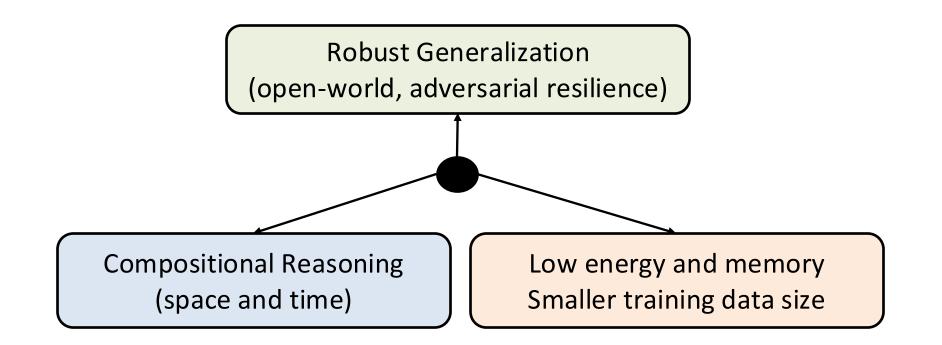
# **Semantic Verification of Foundation Models**

# Susmit Jha

**Technical Director** 

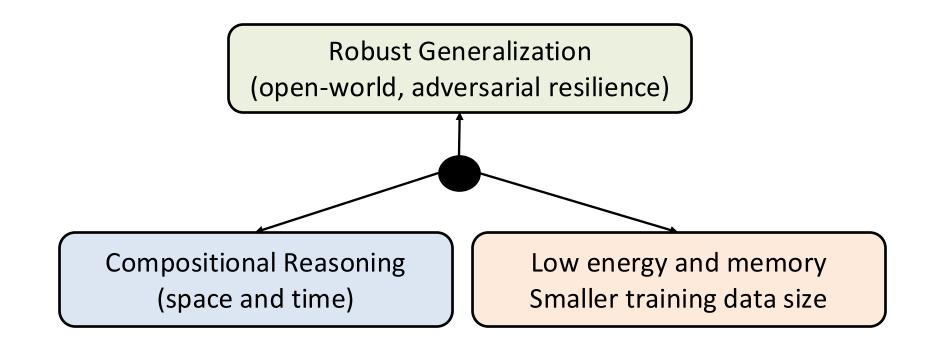
Neuro-symbolic Computing and Intelligence Research Group Information and Computing Sciences Division SRI International

### **Three Major Dimensions of the Challenge of Robust Learning**



No machine learning paradigm can match the plasticity, efficiency, and reasoning capability of the human brain.

### **Three Major Dimensions of the Challenge of Robust Learning**

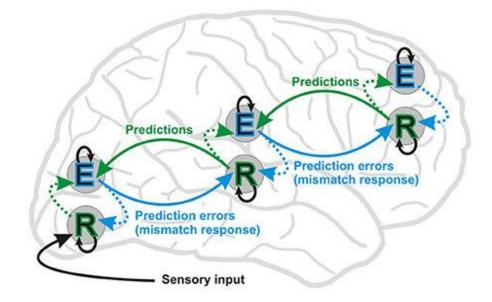


### Central to solving all three challenges together is the ability to abstract and form concepts.

# **Predictive Processing – a Theory of Mind**

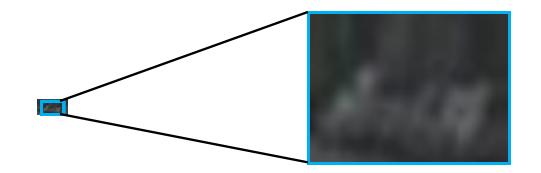
Predictive coding (also known as predictive processing) is a **theory of mind in which the mind is constantly generating and updating a mental model of the environment**. The model is used to generate predictions of sensory input that are compared to actual sensory input.

Rao and Ballard'99, Friston and Kiebel'09 Stefanics et. al.'14



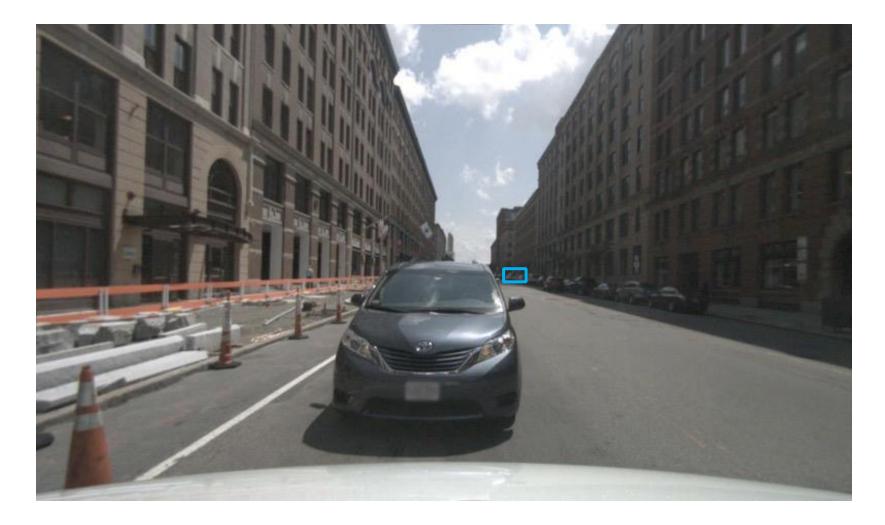
### Human perception is model-based, using our context to bias the interpretation of sensors.

### **Predictive Processing – a Theory of Mind**



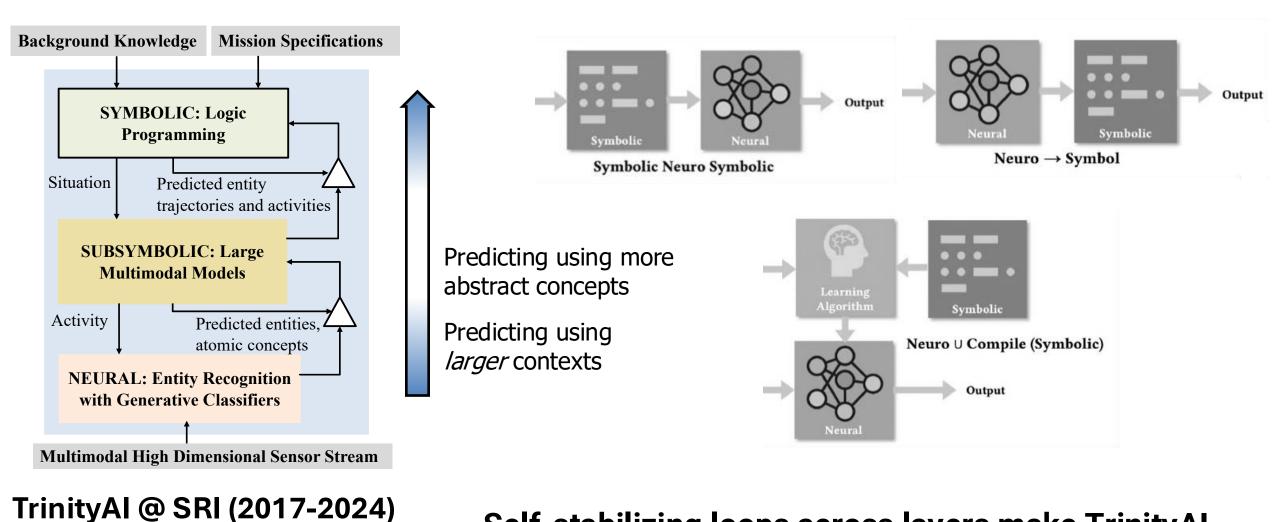
#### Human perception is model-based, using our context to bias the interpretation of sensors.

### **Predictive Processing – a Theory of Mind**



Human perception is model-based, using our context to bias the interpretation of sensors.

# **TrinityAI: Neuro-symbolic Architecture Inspired by Predictive Coding**

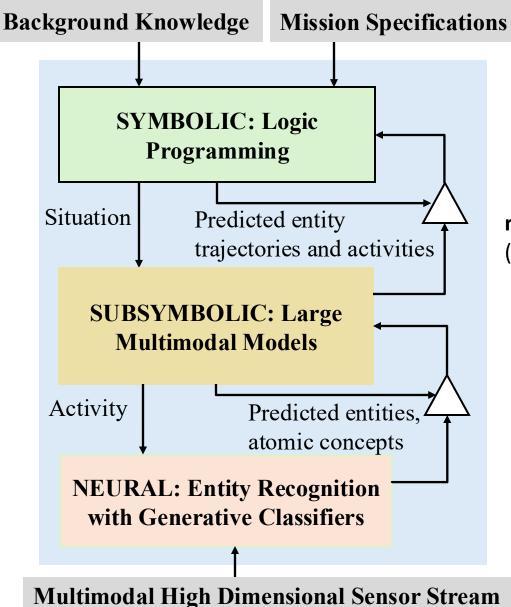


# Self-stabilizing loops across layers make TrinityAl robust to adversarial perturbations.

(DARPA, NSA, ARL, IARPA,

**ARPA-H**)

### **TrinityAI: Learn with Less Data and Robust to OOD perturbations**







movable object

human (19.46%), bicycle (1.04%), **motorcycle (1.11%)**, car (43.62%), truck (12.70%), movable object (22.05%)

#### **Recent References**

- Kaur et. al. AAAI 2022
- Acharya et. al. IJCAI, 2022.
- Cunningham et. al. ICML'22
- Kaur et. al. ICCPS'23
- Gupta et. al. CVPR'23
- Magesh et. al. JMLR'24

| Model                      | Occlusion (%) | Overall  | Class-wise accuracy |         |                 |       |       |                   |
|----------------------------|---------------|----------|---------------------|---------|-----------------|-------|-------|-------------------|
|                            |               | accuracy | human               | bicycle | motor-<br>cycle | car   | truck | movable<br>object |
| CNN - ResNet<br>(Baseline) | No occlusion  | 88.65    | 92.44               | 57.24   | 61.31           | 92.59 | 69.74 | 90.69             |
| CNN - ResNet<br>(Baseline) | 30%           | 83.24    | 90.99               | 12.52   | 20.90           | 92.48 | 71.15 | 71.36             |
| CNN - ResNet<br>(Baseline) | 50%           | 79.17    | 94.93               | 2.36    | 12.48           | 87.33 | 58.94 | 67.95             |
|                            |               |          |                     |         |                 |       |       |                   |
| TrinityAI                  | No occlusion  | 95.51    | 98.38               | 66.25   | 73.37           | 97.13 | 82.17 | 98.62             |
| TrinityAI                  | 30%           | 94.70    | 98.72               | 66.66   | 65.40           | 96.62 | 81.31 | 96.73             |
| TrinityAl                  | 50%           | 93.13    | 97.53               | 31.36   | 64.88           | 94.17 | 82.10 | 96.34             |

# TrinityAI: Uncertainty-quantified prediction over novel contexts

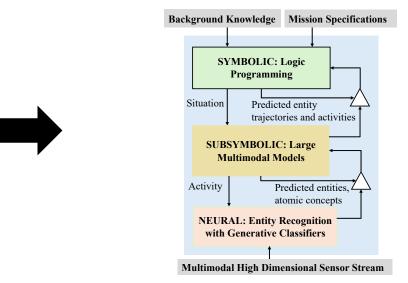
Objects violating common contextual relations, such as co-occurrence, size, and shape relations, in a scene, resulting in compositional novelty.



rup of al "Detecting out of context objects using graph context reasoning network" LICAL 2022

Acharya et. al. "Detecting out-of-context objects using graph context reasoning network." IJCAI 2022.





#### Roy et. al. "Zero-shot Detection of Out-of-Context Objects Using Foundation Models" WACV 2025.

### TrinityAI: Uncertainty-quantified prediction over novel contexts









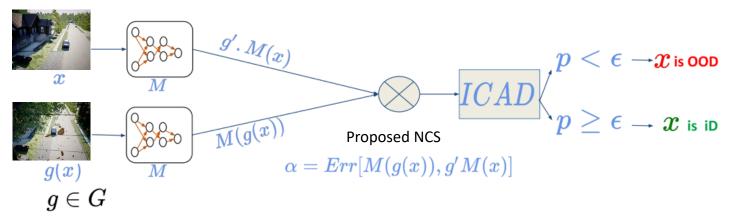


| Dataset     | VLM   | GNN (IJCAI'22) | Ours (WACV'25) |
|-------------|-------|----------------|----------------|
| MIT-OOC     | 23.45 | 73.29          | 90.82          |
| IJCAI22-OOC | 26.78 | 84.85          | 87.26          |

Acharya et. al. "Detecting out-of-context objects using graph context reasoning network." **IJCAI 2022**. Roy et. al. "Zero-shot Detection of Out-of-Context Objects Using Foundation Models" **WACV 2025**.

Neuro-symbolic approach performs better than our prior work with custom-trained GNN without any training and significantly outperforms VLMs.

# TrinityAI: Uncertainty-quantified prediction over longer temporal context



Transform input that is invariant or equivariant and use the difference between the inference between the original and transformed input to compute OOD scores.

Kaur, R. et. al. "iDECODe: In-Distribution Equivariance for Conformal Out-of-Distribution Detection". **AAAI, 2022**. Lin et. al. Safety Monitoring for Learning-Enabled CPS in Out-of-Distribution Scenarios. **ICCPS, 2025**.

Extensions to time series such as videos: Consider temporal transformations such as frame-drop, local reordering, etc.



Kaur, R. et. al. "CODiT: Conformal out-of-distribution Detection in time-series data for cyber-physical systems". **ICCPS**, 2023.

### Failure Cases: Quantitative or Spatial or Temporal Reasoning



087: a silver car that is parked in front of a brick building



063: a refrigerator filled with food and drinks with a white door



219: a man standing on a street corner talking on a cell phone



134: a truck and a taxi are driving down a street



104: a large sign on a gravel road in the middle of a field

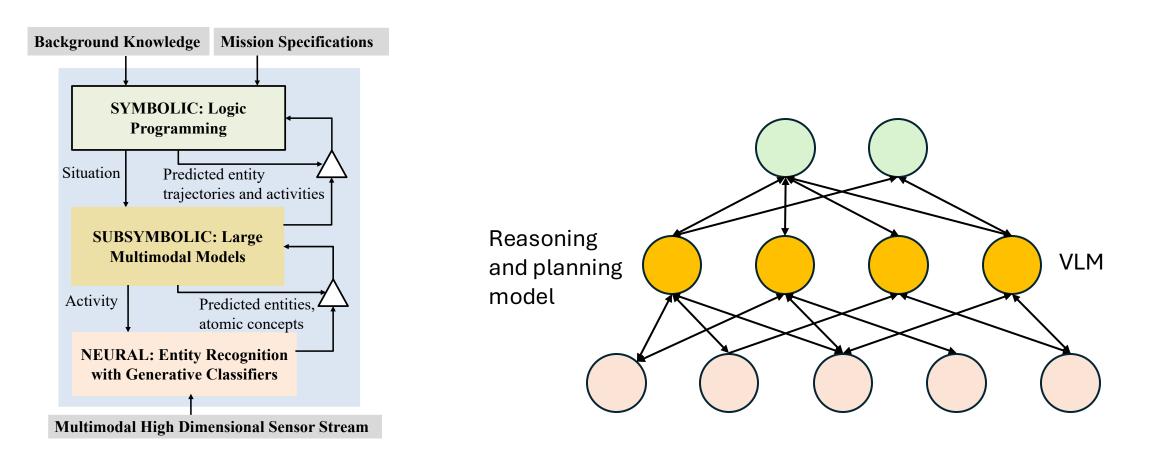


068: a bathroom with a toilet and a wall with a lot of rolls of toilet paper



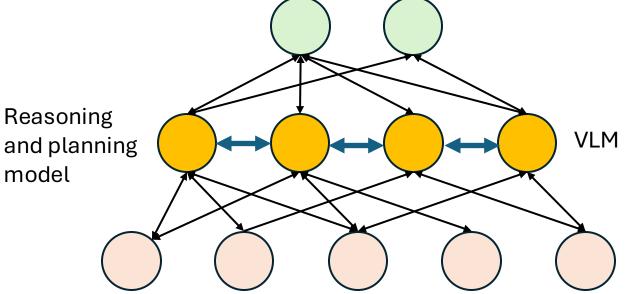
189: a man riding a small motorcycle down a street in front of a house

### Lack of specialized reasoning is a key limitation.

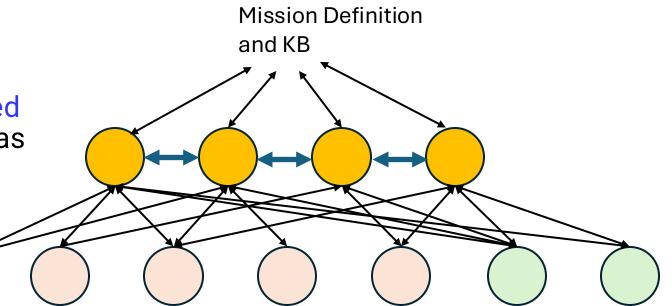


TrinityAl @ SRI (2017-2024) (DARPA, NSA, ARL, IARPA, ARPA-H)

• Foundation Models communicate with each other exchanging inferences and enriching their context.



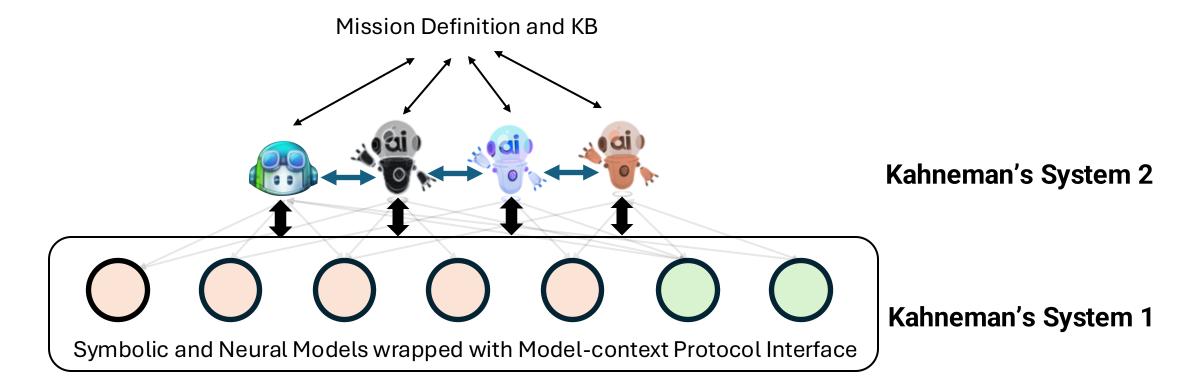
- Foundation Models communicate with each other exchanging inferences and enriching their context.
- Increased context length and improved reasoning makes FMs more suitable as the System 2 top-layer with dedicated reasoning engines available as a tool.



- Exploit tool-calling / MCP to make the architecture self-organizing.
- Train LLMs to decompose complex tasks as simpler tasks that can be solved by lower—level models.
- Assurance by checking consistency of inferences not just across layers but within the same layer.

Mission Definition and KB

SANSHA: Self-organizing Assembly of Neuro-Symbolic Heterogeneous Agents (2024-now: DARPA ANSR, DARPA TIAMAT, ARL IOBT, ARPA-H DIGIHEALS)



### **Connections to Theories on Human Cognition**

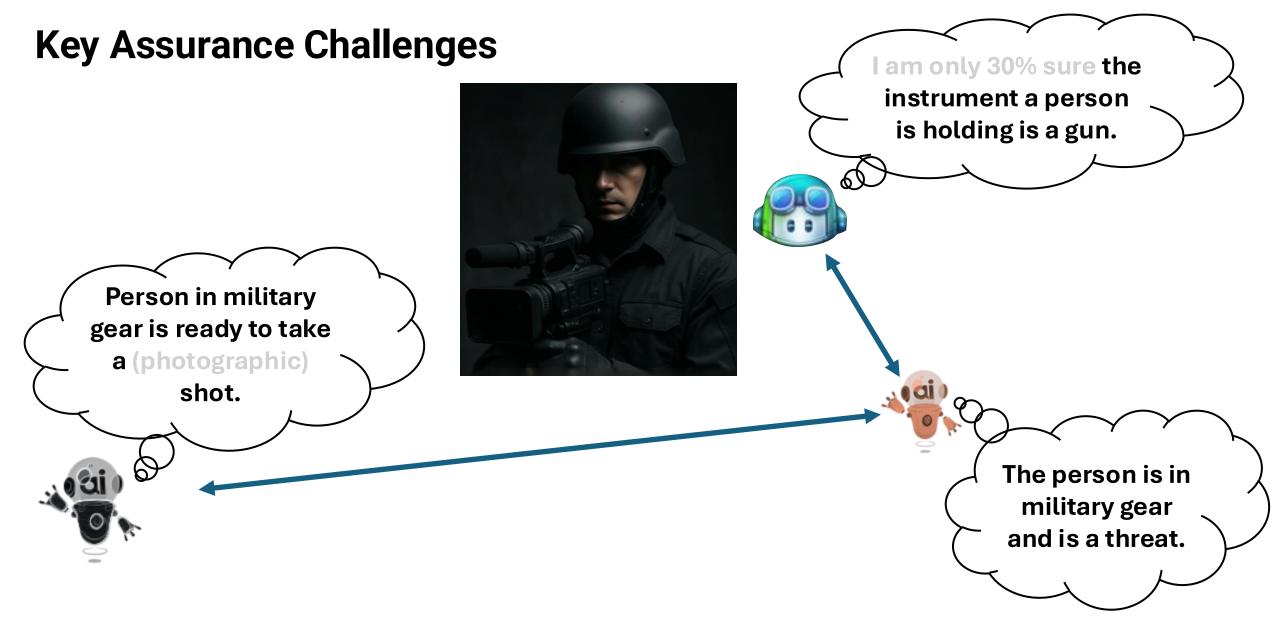


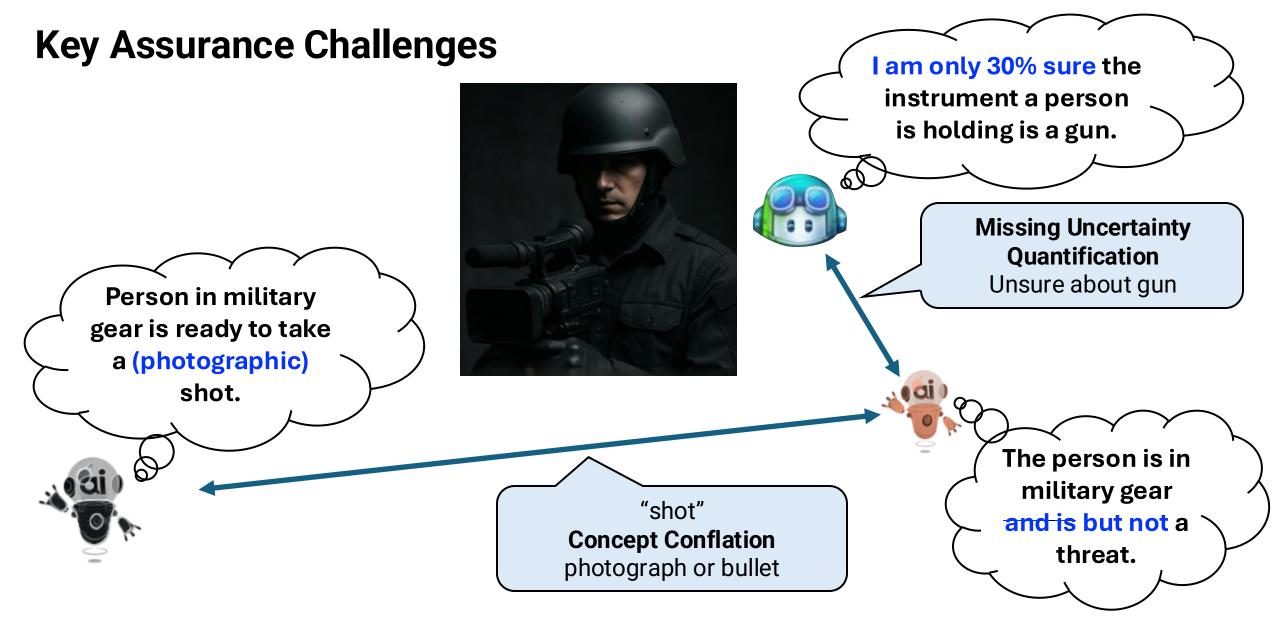
**Marvin Minsky's Society of Mind** – intelligence is a *"vast society of individually simple processes known as agents."* Higher-level reasoning arises when small specialist agents are recruited into larger coalitions, so the deliberative voice is really a negotiated consensus.

**Bernard Baars' Global Workspace Theory (GWT)** – dozens of unconscious processors compete for access to a shared "workspace"; winning coalitions broadcast their data so other modules can join in planning, problem-solving, and verbal report—classic System 2 tasks.

**Daniel Dennett's Multiple Drafts Model** – conscious thought is "a variety of interpretations of inputs," each a "draft" that can gain or lose influence. No single homunculus; what feels like a unitary System 2 is whichever draft wins the editing war.

Several theories argue System 2 is not one homogeneous entity but a committee.

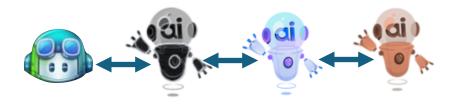




Uncertainty quantification and semantic consistency of concepts are essential.

Susmit Jha

### **Key Assurance Challenges**

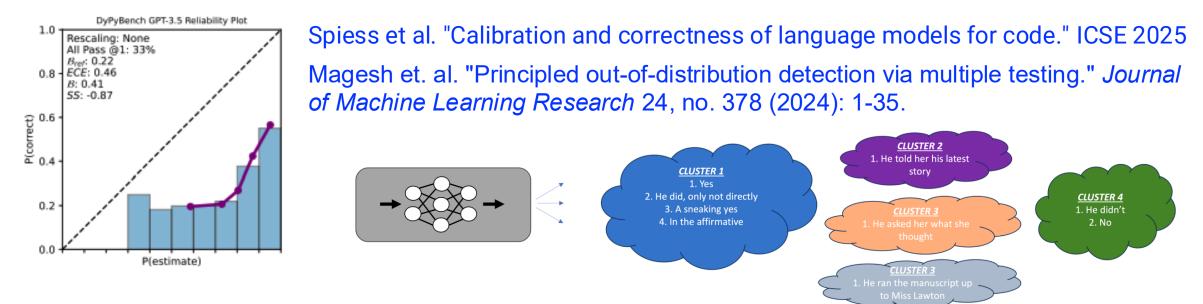


Quantify Uncertainty of Responses

• Verify Concepts in Foundation Models are Aligned Mutually and with Humans

Uncertainty quantification and semantic consistency of concepts are essential.

## **Uncertainty Quantification in Foundation Models: Post-processing**

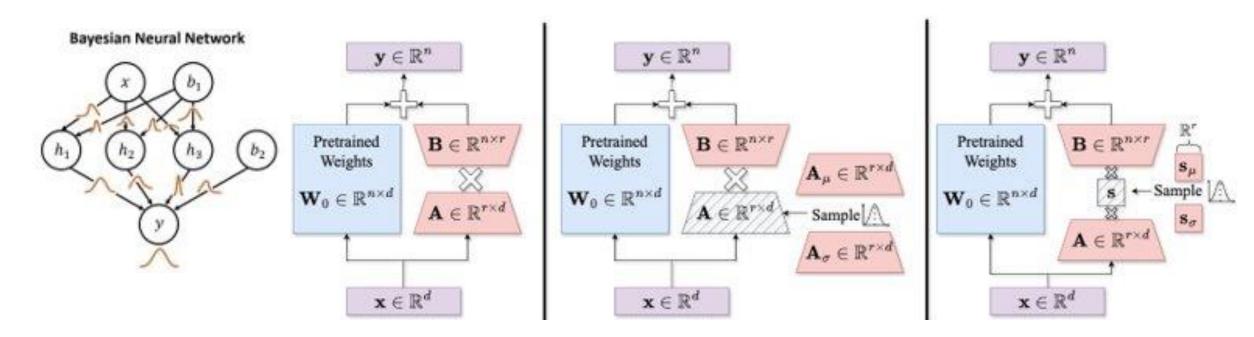


#### LLM Bayesian Post-Processing: Semantic Clustering and Conformal Prediction

|             |         | COQA Dataset |                     |       | TriviaQA Dataset            |       |                     |       |                             |
|-------------|---------|--------------|---------------------|-------|-----------------------------|-------|---------------------|-------|-----------------------------|
| Model Eval. |         | Model        | Sem. Ent.           | EigV  | Ours                        | Model | Sem. Ent.           | EigV  | Ours                        |
|             |         | Acc.         | Unnorm/Norm         |       | Unnorm/Norm                 | Acc.  | Unnorm/Norm         |       | Unnorm/Norm                 |
| Llama-13b   | GPT-4   | 73.22        | 85.81/86.44         | 88.03 | 86.35/ <u>87.47</u>         | 67.03 | 88.13/87.94         | 88.84 | 88.33/ <u>88.54</u>         |
| Mistral-7b  | GPT-4   | 73.38        | 81.91/82.68         | 82.82 | 82.22/ <b>82.95</b>         | 60.68 | 80.99/ <u>81.40</u> | 82.03 | 81.23/ <b>82.03</b>         |
| Mean        | GPT-4   | 73.30        | 83.86/84.56         | 85.43 | 84.29/ <u>85.21</u>         | 63.86 | 84.56/84.67         | 85.44 | 84.78/ <u>85.29</u>         |
| Llama-13b   | RougeL  | 72.75        | 86.03/87.05         | 87.92 | 86.84/ <b>88.34</b>         | 64.60 | 85.62/85.19         | 85.76 | <u>85.86</u> / <b>85.87</b> |
| Mistral-7b  | RougeL  | 44.74        | <u>64.37</u> /62.93 | 63.43 | <b>64.60</b> /63.48         | 42.33 | <u>70.18</u> /68.13 | 69.41 | <b>70.26</b> /68.81         |
| Mean        | RougeL  | 58.75        | 75.20/74.99         | 75.65 | <u>75.72</u> / <b>75.91</b> | 53.47 | <u>77.90</u> /76.66 | 77.59 | <b>78.06</b> /77.34         |
| Llama-13b   | Deberta | 63.74        | 80.21/79.48         | 82.68 | 81.04/ <u>81.37</u>         | 63.33 | 84.92/84.34         | 85.60 | <u>85.23</u> /85.13         |
| Mistral-7b  | Deberta | 11.23        | <u>23.56</u> /20.71 | 20.88 | <b>23.53</b> /21.05         | 33.92 | <u>62.29</u> /59.53 | 60.39 | <b>62.37</b> /60.16         |
| Mean        | Deberta | 37.49        | <u>51.89</u> /50.10 | 51.78 | <b>52.29</b> /51.21         | 48.63 | <u>73.61</u> /71.94 | 73.00 | <b>73.80</b> /72.65         |

Kaur et. al. Enhancing Semantic Clustering for Uncertainty Quantification & Conformal Prediction by LLMs. Statistical Frontiers in LLMs and Foundation Models, 2024

### **Uncertainty Quantification in Foundation Models: Bayesian LORA**

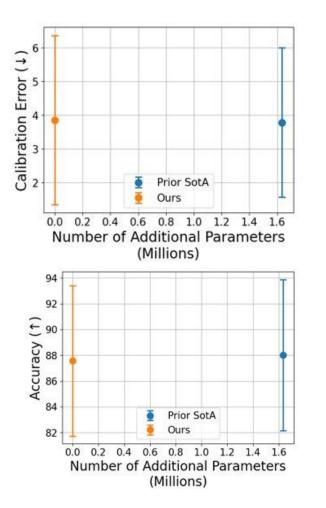


LLM Bayesian Finetuning: Bayesian LORA (under submission to UAI)

d is the embedding dimension of the model and n is the output dimension of the layer.

A combination of finetuning with uncertainty quantification LORA adaptors and post-hoc consistency analysis can help detect when foundation models are confabulating/hallucinating.

## **Uncertainty Quantification in Foundation Models: Bayesian LORA**

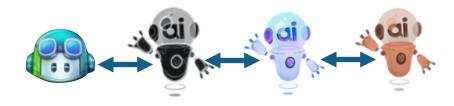


|         |                |            |                            |                               | Datasets                     |                              |                             |
|---------|----------------|------------|----------------------------|-------------------------------|------------------------------|------------------------------|-----------------------------|
| Metric  | Method         | Params (M) | In Dist.                   | Smaller I                     | Dist. Shift                  | Larger D                     | ist. Shift                  |
|         |                |            | OBQA                       | ARC-C                         | ARC-E                        | Chemistry                    | Physics                     |
|         | MLE            | 3.768      | 91.70 $_{\pm 0.2}$         | $90.15_{\pm 0.8}$             | $95.31_{\pm0.3}$             | $53.33_{\pm 1.2}$            | $54.17_{\pm 2.5}$           |
|         | MAP            | 3.768      | $91.60_{\pm 0.2}$          | $90.43_{\pm 1.1}$             | $95.48_{\pm0.4}$             | $53.33_{\pm 1.2}$            | $56.00_{\pm 1.7}$           |
|         | MC-Droput      | 3.768      | $91.80_{\pm 0.7}$          | $90.09_{\pm0.5}$              | $95.54_{\pm 0.4}$            | $52.00_{\pm 2.6}$            | $52.67_{\pm 1.2}$           |
| ACC (†) | Ensemble       | 11.305     | $92.53_{\pm 0.5}$          | $90.32_{\pm0.4}$              | $95.13_{\pm0.1}$             | $52.67_{\pm 0.6}$            | $54.33_{\pm 1.2}$           |
|         | Laplace        | 3.768      | $91.60_{\pm 0.7}$          | $90.62_{\pm 0.4}$             | $95.82_{\pm 0.2}$            | $48.33_{\pm 3.0}$            | $47.71_{\pm 0.6}$           |
|         | BLoB           | 5.403      | $91.67_{\pm 0.8}$          | <b>92.82</b> $_{\pm 0.5}$     | $95.95_{\pm 0.2}$            | <b>55.21</b> <sub>±1.8</sub> | $53.47_{\pm 1.6}$           |
|         | ScalaBL (ours) | 3.769      | $90.60_{\pm 0.3}$          | $\underline{91.55}_{\pm 0.4}$ | $95.54_{\pm 0.4}$            | $52.43_{\pm 3.0}$            | $53.82_{\pm 1.6}$           |
|         | MLE            | 3.768      | $6.50_{\pm 0.3}$           | $8.11_{\pm 0.7}$              | $3.58_{\pm0.3}$              | $23.66_{\pm 1.3}$            | $22.65_{\pm 3.4}$           |
|         | MAP            | 3.768      | $6.40_{\pm 0.3}$           | $7.99_{\pm 1.0}$              | $3.38_{\pm0.2}$              | $24.01_{\pm 1.9}$            | $22.36_{\pm 4.6}$           |
|         | MC-Dropout     | 3.768      | $6.55_{\pm 0.2}$           | $8.22_{\pm 0.9}$              | $3.28_{\pm0.5}$              | $24.54_{\pm 2.9}$            | $20.51_{\pm 2.3}$           |
| ECE (↓) | Ensemble       | 11.305     | $4.65_{\pm 0.4}$           | $6.50_{\pm0.4}$               | $3.00_{\pm 0.4}$             | $19.78_{\pm 1.7}$            | $16.73_{\pm 2.2}$           |
|         | Laplace        | 3.768      | $2.47_{\pm 0.4}$           | $4.56_{\pm 1.0}$              | $\underline{2.06}_{\pm 0.2}$ | $15.62_{\pm 3.1}$            | $11.66_{\pm 0.3}$           |
|         | BLoB           | 5.403      | $2.46_{\pm 0.8}$           | $\underline{4.54}_{\pm 0.3}$  | $2.50_{\pm 0.3}$             | $15.16_{\pm 1.1}$            | $16.62_{\pm 2.2}$           |
|         | ScalaBL (ours) | 3.769      | $2.38_{\pm 0.8}^{\pm 0.8}$ | $4.29_{\pm 1.2}^{\pm 0.0}$    | $1.85_{\pm0.4}$              | $16.59_{\pm 2.3}$            | $17.23_{\pm 0.9}$           |
|         | MLE            | 3.768      | $0.38_{\pm 0.0}$           | $0.47_{\pm 0.0}$              | $0.23_{\pm 0.0}$             | $1.55_{\pm 0.0}$             | $1.20_{\pm 0.0}$            |
| NLL (↓) | MAP            | 3.768      | $0.37_{\pm 0.0}$           | $0.46_{\pm0.1}$               | $0.22_{\pm 0.0}$             | $1.56_{\pm 0.0}$             | $1.21_{\pm0.0}$             |
|         | MC-Dropout     | 3.768      | $0.36_{\pm0.0}$            | $0.47_{\pm0.0}$               | $0.22_{\pm 0.0}$             | $1.53_{\pm 0.1}$             | $1.21_{\pm0.1}$             |
|         | Ensemble       | 11.305     | $0.27_{\pm 0.0}$           | $0.34_{\pm0.0}$               | $0.18_{\pm0.0}$              | $1.31_{\pm0.0}$              | $1.08_{\pm0.0}$             |
|         | Laplace        | 3.768      | $0.24_{\pm 0.0}$           | $0.31_{\pm 0.0}$              | $0.15_{\pm 0.0}$             | $1.11_{\pm 0.0}$             | $1.04_{\pm0.0}$             |
|         | BLoB           | 5.403      | $0.21_{\pm 0.0}$           | $0.27_{\pm 0.0}$              | $0.16_{\pm 0.0}$             | $1.33_{\pm 0.1}$             | $0.99_{\pm 0.0}$            |
|         | ScalaBL (ours) | 3.769      | $0.23_{\pm 0.0}$           | $\underline{0.26}_{\pm 0.0}$  | $0.14_{\pm 0.0}$             | $1.25_{\pm 0.0}$             | $\overline{0.94}_{\pm 0.0}$ |

Our approach Bayesian LORA can achieve 0.76 ECE performance with the same accuracy requiring 1792X less additional parameters than SOTA.

A combination of finetuning with uncertainty quantification LORA adaptors and post-hoc consistency analysis can help detect when foundation models are confabulating/hallucinating.

### **Key Assurance Challenges**

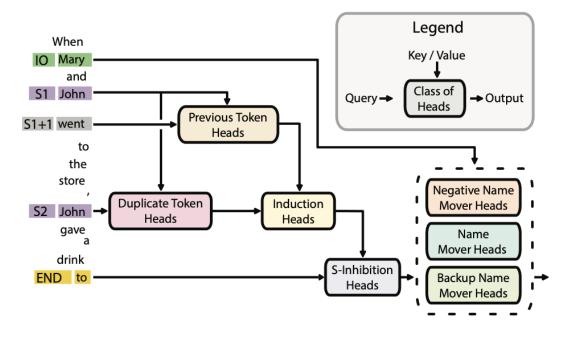


Quantify Uncertainty of Responses

• Verify Concepts in Foundation Models are Aligned Mutually and with Humans

### Uncertainty quantification and semantic consistency of concepts are essential.

### **Mechanistic Interpretability**



### **Mechanistic View**

Approach: Bottom-up

Algorithmic Level: Node-to-node connections

Implementational Level: Neurons, pathways, circuits

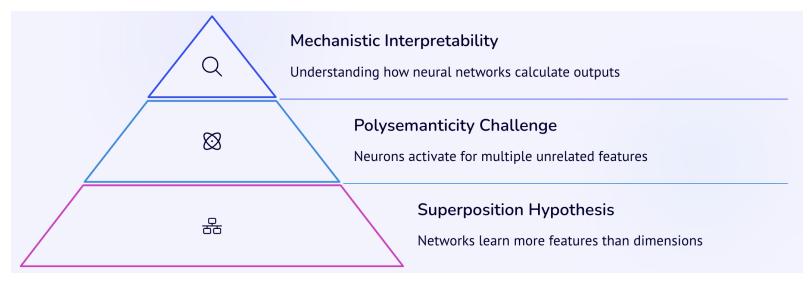
#### Neuron-level analysis

Anthropic's Sparse AutoEncoders [Cunningham et al., 2023] Scaling & Evaluating SAEs, OpenAI 2024 Towards Principled Evaluations of SAEs, Google 2024 Route SAEs to interpret LLMs [Shi et al., 2025]

#### Model-level analysis

Mechanistic Unveiling of Transformer Circuits [Zhang, 2025] The optimal BERT surgeon [Kurtic et al., 2022] Automated Circuit Discovery [Conmy et al., 2023] Circuit Discovery with Graph Pruning [Yu et al., 2024]

### **Concept Probes: Superposition and Polysemantic Representation**



**Knowledge Graphs as Data Foundation** 

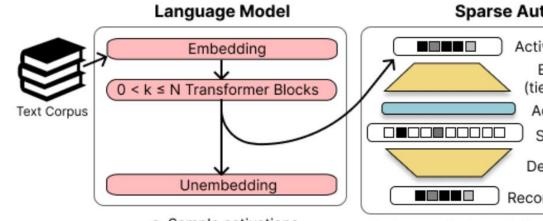
Knowledge Graphs like ConceptNet provide rich information on entities (nodes) and their relationships (edges). To our knowledge, KGs have only been used to add context to input queries (RAG-technique) for improving LLM performance, not for mechanistic interpretability

#### Logical Language Representation

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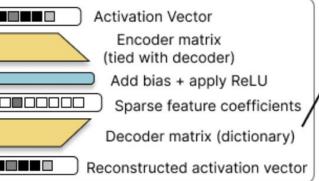
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We extract KG information and store it in logical language format with entities as predicates and relationships as connectors between predicates



a. Sample activations from a language model

#### Sparse Autoencoder



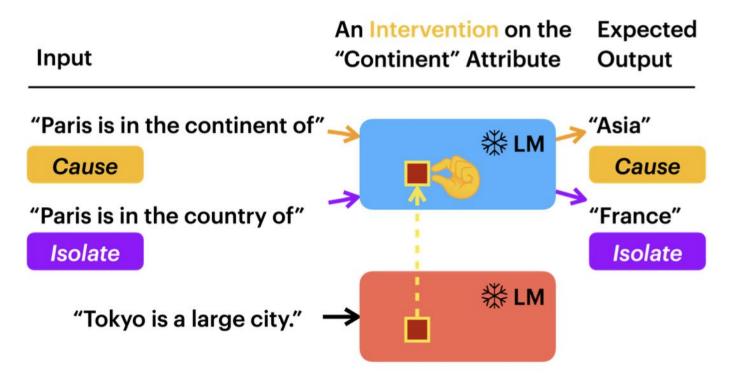
b. Learn a feature dictionary using an autoencoder that learns to represent activation vectors as a sparse linear combination of feature vectors.

#### Feature Dictionary

|             | Feature | Meaning               | Interpretability<br>Score |
|-------------|---------|-----------------------|---------------------------|
| 7           | k-0001  | Words ending in "ing" | 0.56                      |
| $^{\prime}$ | k-xxxx  |                       |                           |
|             | k-2048  | Chemistry terms       | 0.38                      |

c. Interpret the resulting dictionary features

### **Concept Probes: Superposition and Polysemantic Representation**



#### **Knowledge Graphs as Data Foundation** 윪

Knowledge Graphs like ConceptNet provide rich information on entities (nodes) and their relationships (edges). To our knowledge, KGs have only been used to add context to input queries (RAG-technique) for improving LLM performance, not for mechanistic interpretability

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#### Logical Language Representation

We extract KG information and store it in logical language format with entities as predicates and relationships as connectors between predicates

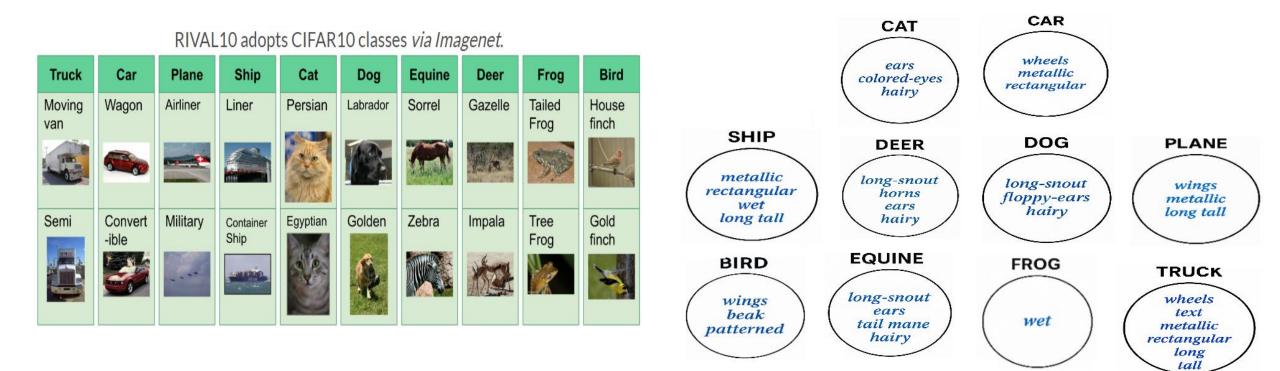
#### **Compositional Concepts**

What is the national language of the country where Paris is located?

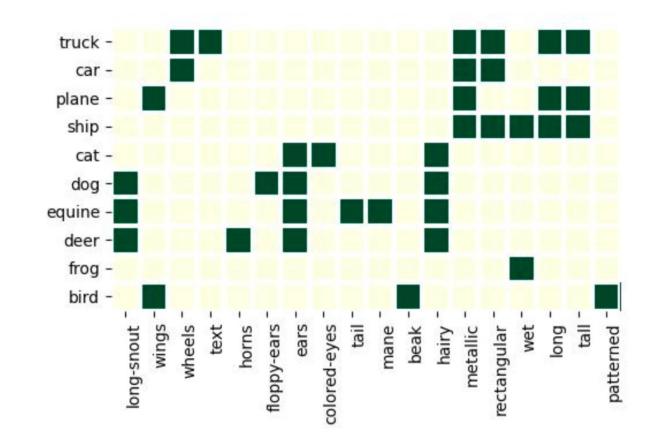
What is the national language of the country where London is located?

### **Datasets with Ground-truth Concepts for Evaluation**

RIVAL-10 (Rich Visual Attributes with Localization) dataset [Moayeri et. al, CVPR'22]



### **Datasets with Ground-truth Concepts for Evaluation**



RIVAL-10 (Rich Visual Attributes with Localization) dataset [Moayeri et. al, CVPR'22]

Birds(x) :- in(a1,x), wings(a1), in(a2, x), beak(a2), in(a3,x), patterned(a3)

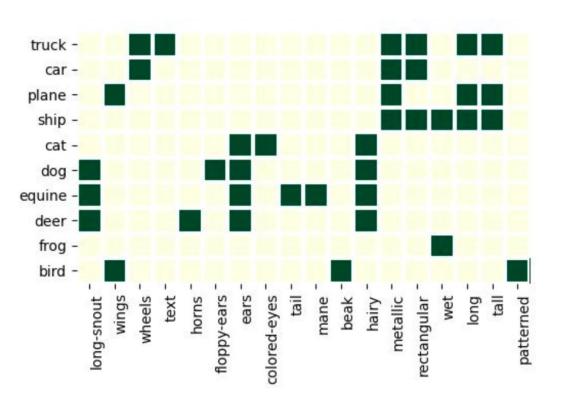
Susmit Jha

### **Foundation Model Semantic Verification Property Language**

Semantic Specification Language

 $\begin{array}{ll} (\text{variables}) & x \in Vars\\ (\text{concept names}) \ con_1, \ con_2 \in Concepts\\ (\text{classes}) & c \in C \end{array}$   $E ::= > (x, \ con_1, \ con_2) | \ predict(x, \ c) | \neg E | \ E \land E | \ E \lor E$   $hasCon(x, \ con) := \bigwedge_{con_i \in Concepts \ \land \ con_i \neq con} \land (x, \ con_i, \ con_i)$ 

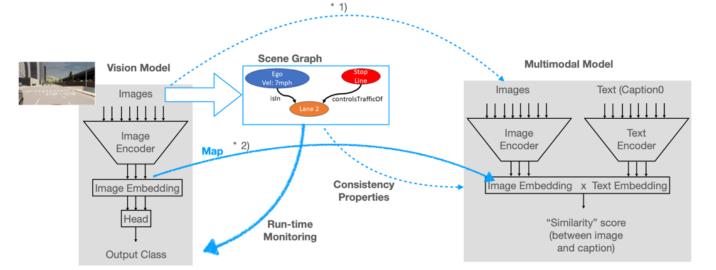
 $\begin{array}{ll} (\operatorname{Con}_{\operatorname{spec}} \ \operatorname{expressions}) & e \in E \\ (\operatorname{classifiers}) & f \in F := \mathbb{R}^d \to \mathbb{R}^{|C|} \\ (\operatorname{inputs}) & v \in X := \mathbb{R}^d \\ (\operatorname{concept representation maps}) \ rep \in Rep := Concepts \to (\mathbb{R}^d \to \mathbb{R}) \\ (\operatorname{semantics}) \ \llbracket e \rrbracket \in F \times X \times Rep \to \{\operatorname{True}, \operatorname{False}\} \\ \llbracket > (x, \operatorname{con}_1, \operatorname{con}_2) \rrbracket (f, v, rep) := \operatorname{rep}(\operatorname{con}_1)(v) > \operatorname{rep}(\operatorname{con}_2)(v) \\ \llbracket \operatorname{predict}(x, c) \rrbracket (f, v, rep) := (\operatorname{argmax}(f(v)) = \{c\}) \\ \llbracket \neg e \rrbracket (f, v, rep) := \neg \llbracket e \rrbracket (f, v, rep) \\ \llbracket e_1 \wedge e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \land \llbracket e_2 \rrbracket (f, v, rep) \\ \llbracket e_1 \lor e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \llbracket e_1 \lor e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \llbracket e_1 \lor e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \llbracket e_1 \lor e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \llbracket e_1 \lor e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \llbracket e_1 \lor e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \llbracket e_1 \lor e_2 \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_1 \rrbracket (f, v, rep) \\ \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_2 \rrbracket (f, v, rep) \\ \rrbracket (f, v, rep) := \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_1 \rrbracket (f, v, rep) \\ \rrbracket (f, v, rep) \lor \rrbracket (f, v, rep) \lor \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_1 \rrbracket (f, v, rep) \lor \llbracket e_1 \rrbracket (f, v, rep) \lor \rrbracket (f, v, r$ 



### **Semantic Verification Using Concept Mapping**

 $r_{map}(z) := Mz + d$ 

$$M, d = \underset{M, d}{\operatorname{argmin}} \frac{1}{|D_{\text{train}}|} \sum_{x \in D_{\text{train}}} \|Mf_{enc}(x) + d - g_{enc}^{img}(x)\|_2^2.$$



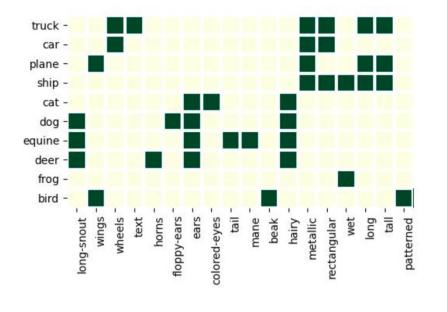
**Definition 4 (Faithful alignment of representation spaces).** Given an encoder  $f_{enc}: X \to Z_f$  of a vision model and an image encoder  $g_{enc}^{img}: X \to Z_g$  of a VLM g, the representation space of  $f_{enc}$  is faithfully aligned with the representation space of  $g_{enc}^{img}$  if there exists a map  $r_{map}: Z_f \to Z_g$  such that,

 $\forall x \in X. r_{map}(f_{enc}(x)) = g_{enc}^{img}(x)$ 

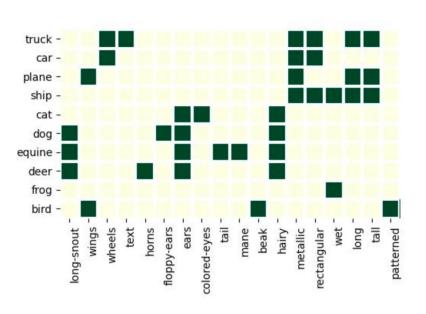
**Theorem 1.** Given a vision model  $f: X \to Y$  with encoder  $f_{enc}: X \to Z_f$ , and a VLM g with encoders  $g_{enc}^{img}: X \to Z$  and  $g_{enc}^{txt}: T \to Z$ , if the representation space of  $f_{enc}$  is faithfully aligned with the representation space of  $g_{enc}^{img}$ , then the linear concept representation map, rep, via VLM g can be defined as,

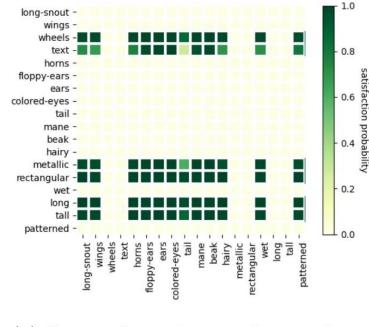
$$rep(con) := \lambda x.cos(r_{map}(f_{enc}(x)), \overline{con})$$

where  $\overline{con}$  is a vector in  $Z_g$  whose direction corresponds to concept con.

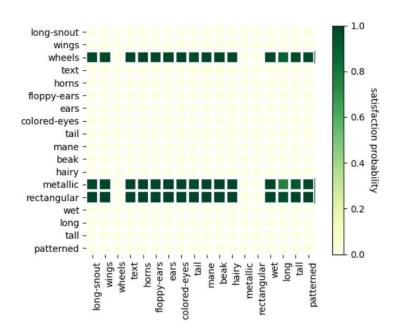


### Semantic Verification of Learned Concepts: Relative Comparison





(a) Strength predicates for *truck* 



(b) Strength predicates for *car* 

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We can specify and verify semantic properties over concepts and check for consistency of representation between two models.

### **Semantic Verification of Concepts: Relative Comparison**

Quantitative Measure of Satisfying Spec

 $predict(c) \implies con_1 > con_2$ 

$$l_{i} \leq w_{i} \leq u_{i}, [l_{i}, u_{i}] \in \overline{B}, \forall i = \{1, ..., p\}$$

$$0 \leq \sum_{i} (A_{c,i} - A_{c_{k},i}) w_{i} + (b_{c} - b_{c_{k}}), \forall c_{k} \neq c$$

$$z_{j} = \sum_{i} M_{j,i} w_{i} + d_{j}, i, j \in \{1, ..., p\}$$

$$\sum_{i} \frac{z_{i}}{\|z\|} \frac{q_{i}^{con_{2}}}{\|q^{con_{2}}\|} > \sum_{i} \frac{z_{i}}{\|z\|} \frac{q_{i}^{con_{1}}}{\|q^{con_{1}}\|}$$

$$\sum_{i} \frac{q_{i}^{con_{2}}}{\|q^{con_{2}}\|} > \varepsilon + \sum_{i} z_{i} \frac{q_{i}^{con_{1}}}{\|q^{con_{1}}\|}$$

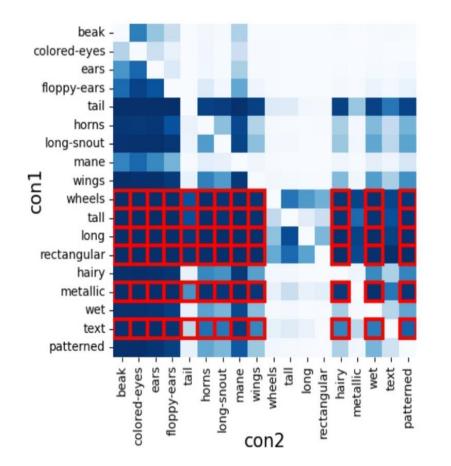
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### **Semantic Verification of Concepts: Relative Comparison**

Heatmap is a visual representation of the concept predicates satisfied by a group of inputs

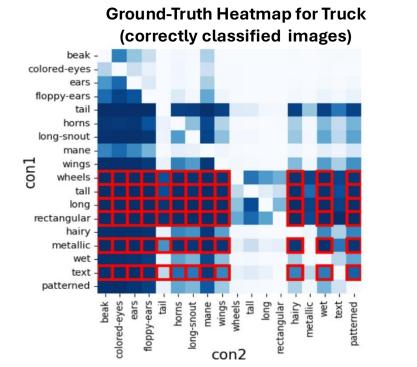
- Darker color indicates higher satisfaction probability
- Cells with red outline are for predicates with relevant concept > irrelevant concept
- Ex. for truck images, the concept-predicates with high satisfaction probabilities are wheels > beak, metallic > mane, text > ears so on

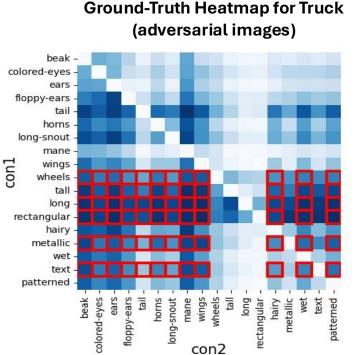
#### Ground-Truth Summary HeatMap (images with GT truck)

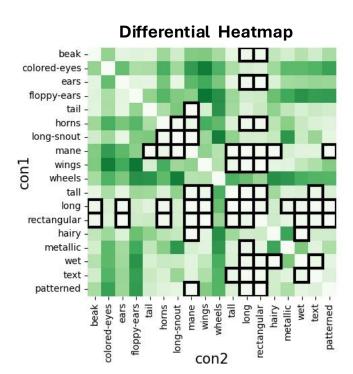


Aggregate summary of concept representation in a model and its consistency with subconcepts.

### Semantic Verification of Concepts: Identifying Conceptual Gaps







#### Predicates for truck that are non-robust: eg. wheels > tail, wheels > floppy-ears, metallic > long-snout

### Semantic Verification of Concepts: Localizing Errors

ground-truth class: ship



Encoder Error CLIP: ship, ResNet18: frog, CLIP via rmap : frog



Head Error CLIP: ship, ResNet18: dog, CLIP via rmap : ship

ground-truth class: cat



Encoder Error CLIP: cat, ResNet18: dog, CLIP via rmap: dog Head Error CLIP: cat, ResNet18: equine, CLIP via Imap : cat ground-truth class: dog



Encoder Error ne, CLIP:dog, ResNet18: equine, CLIP via Imap : equine

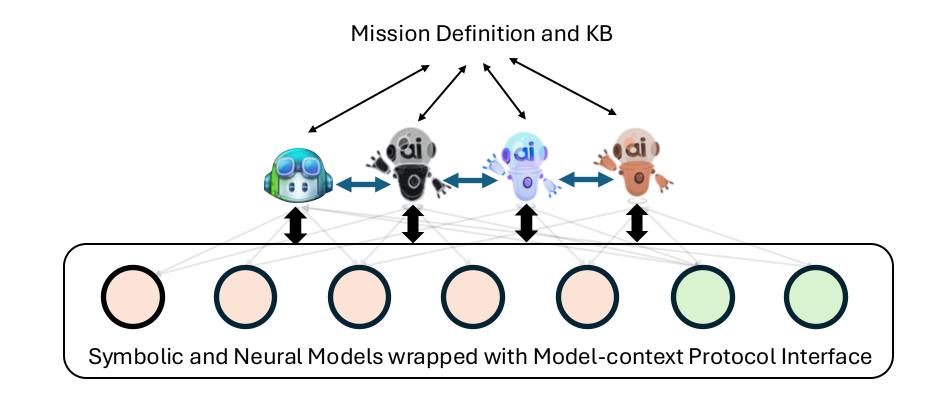


Head Error CLIP: dog, ResNet18: cat, CLIP via rmap : dog

|                                 | -                  |                    |
|---------------------------------|--------------------|--------------------|
| Mutation location               | # encoder error    | # head error       |
| No mutation (original ResNet18) | 61                 | 84                 |
| Mutation in Encoder             | 4271               | 405                |
| Mutation in Head                | 101                | 4571               |
|                                 | 1183 (orig decomp) | 3064 (orig decomp) |
| Mutation in Residual Block 3    | 438 (alt decomp)   | 3809 (alt decomp)  |

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### Assured Self-organizing Assembly of Neuro-Symbolic Heterogeneous Agents

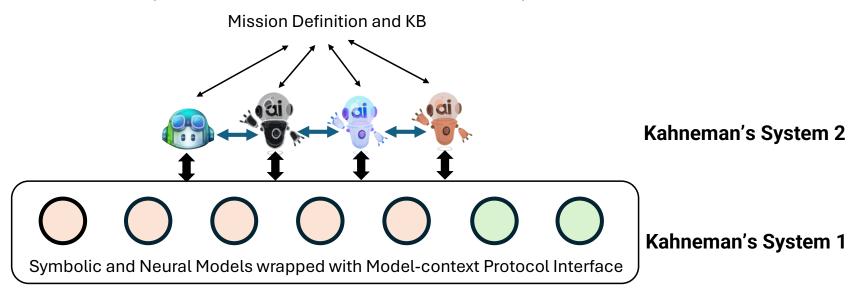


### Uncertainty quantification and semantic consistency of concepts are essential.

Susmit Jha

### Thank you!

#### SANSHA: Self-organizing Assembly of Neuro-Symbolic Heterogeneous Agents (DARPA ANSR, DARPA TIAMAT, ARL IoBT)



- Quantify Uncertainty of Responses
- Verify Concepts in Foundation Models are Aligned Mutually and with Humans

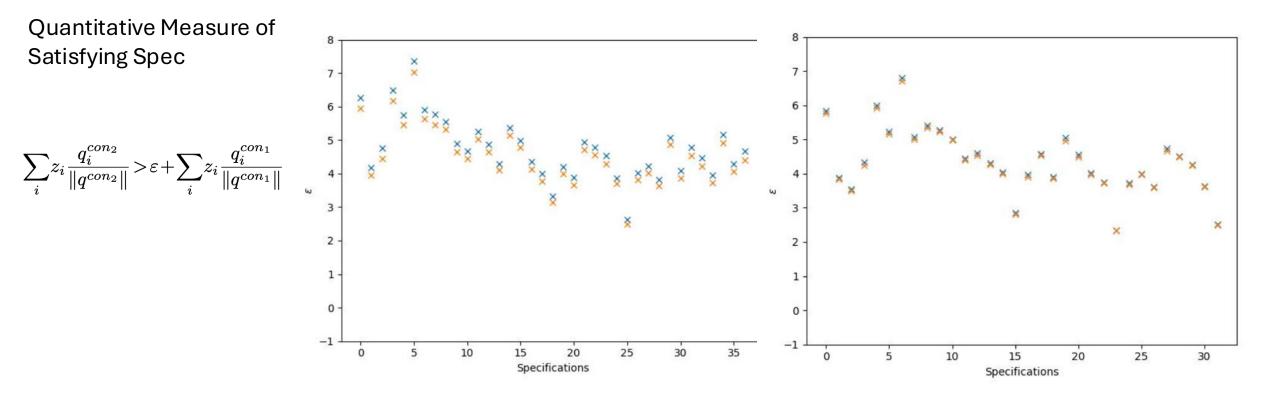
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### **Semantic Verification of Concepts**



Specification 25 that has the lowest value for the violation measure ε suggesting that if the ResNet18 model predicts truck, it likely that rectangular>patterned holds; specification 5 suggests that wheels>colored-eyes is less likely.

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